

§ 4.6 Transformations of Exponential Functions

Let us start with the parent function $f(x) = 2^x$. We will now look at transformations using the function:

$$g(x) = af(k(x-d))+c$$

where f is the function, a, k, d , and c are variables which change the location or shape of the graph $f(x)$.

We will now investigate these variables in terms of $f(x) = b^x$.

For now, we will let $b = 2$. Let's refer to *GSP* to see what a, k, d and c do. Since the function is an exponential, the above function will appear as:

$$g(x) = ab^{(k(x-d))+c}$$

Notes about: $g(x) = ab^{(k(x-d))}+c$

You will notice that if $g(x)$ has only an "a" and/or "k" and/or d transformation(s), the asymptote is the same as the parent function located at $f(x)=0$.

"c" transformations raise or lower the parent's asymptote "c" units.

The domain of the function, regardless of the transformation(s) is *ALWAYS* $\{x \in \mathbb{R}\}$.

The range is only affected by "c" transformations. In essence, the range can be written as $\{f(x) \in \mathbb{R} \mid f(x) < c\}$ or $\{f(x) \in \mathbb{R} \mid f(x) > c\}$, depending on "k".

Homework: §4.6#1-3,5,7-9,11